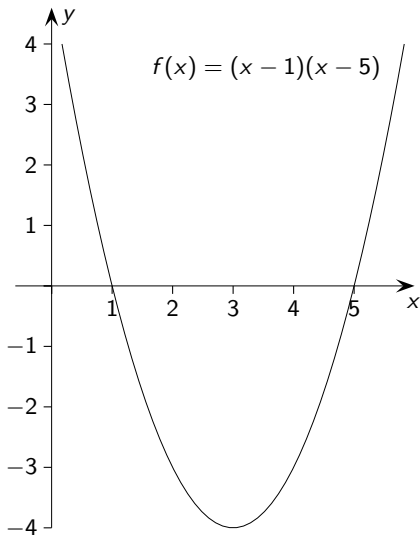


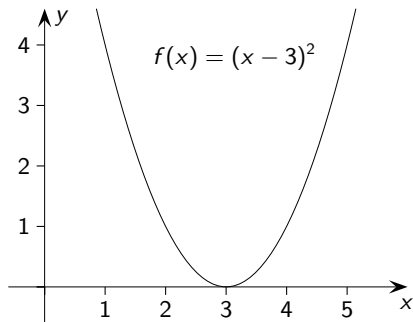
Zerlegung in Linearfaktoren

grooofs.de

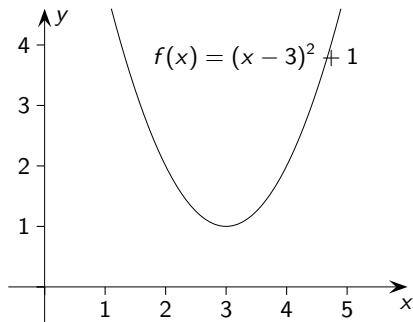
Polynom 2. Grades $ax^2 + bx + c$



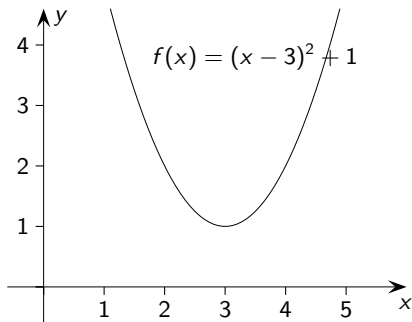
Polynom 2. Grades $ax^2 + bx + c$



Polynom 2. Grades $ax^2 + bx + c$

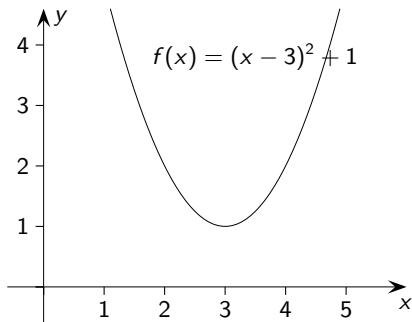


Polynom 2. Grades $ax^2 + bx + c$



Die Zerlegung eines Polynoms 2. Grades richtet sich nach der Anzahl der Nullstellen (2, 1 oder 0) der zugehörigen Polynomfunktion (Parabel).

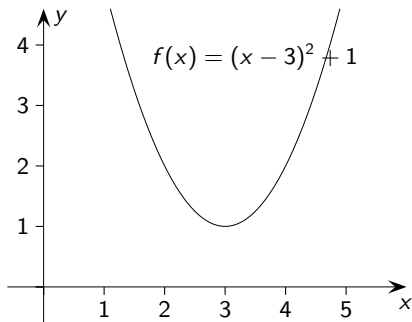
Polynom 2. Grades $ax^2 + bx + c$



Die Zerlegung eines Polynoms 2. Grades richtet sich nach der Anzahl der Nullstellen (2, 1 oder 0) der zugehörigen Polynomfunktion (Parabel).

Für 2 Nullstellen gilt z. B.: $3x^2 - 18x + 15 = 3(x^2 - 6x + 5) = 3(x - 1)(x - 5)$

Polynom 2. Grades $ax^2 + bx + c$

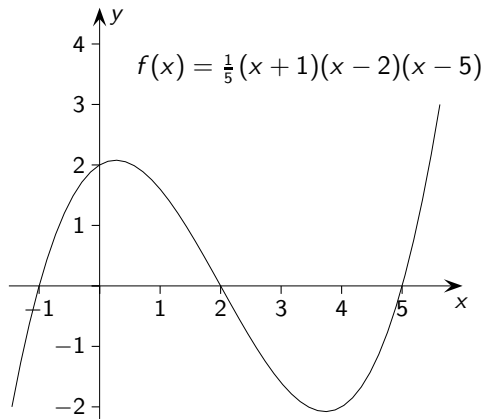


Die Zerlegung eines Polynoms 2. Grades richtet sich nach der Anzahl der Nullstellen (2, 1 oder 0) der zugehörigen Polynomfunktion (Parabel).

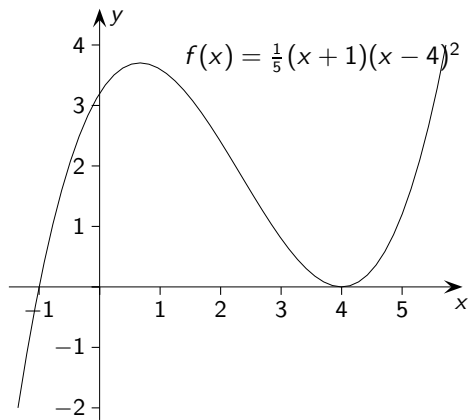
Für 2 Nullstellen gilt z. B.: $3x^2 - 18x + 15 = 3(x^2 - 6x + 5) = 3(x - 1)(x - 5)$

$(x - 3)^2 + 1$ kann nicht in Linearfaktoren zerlegt werden.

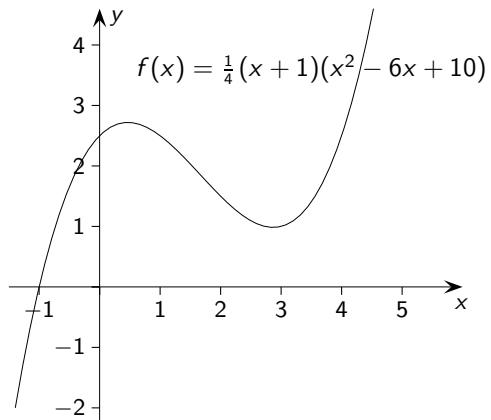
Polynom 3. Grades $ax^3 + bx^2 + cx + d$



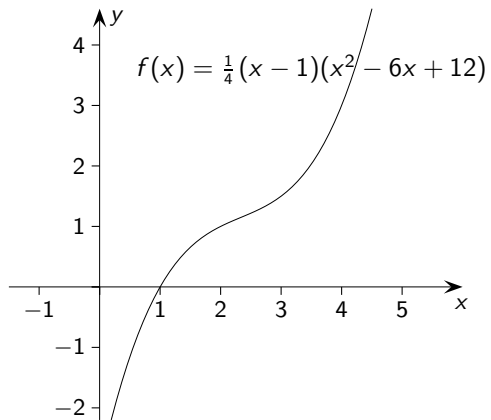
Polynom 3. Grades $ax^3 + bx^2 + cx + d$



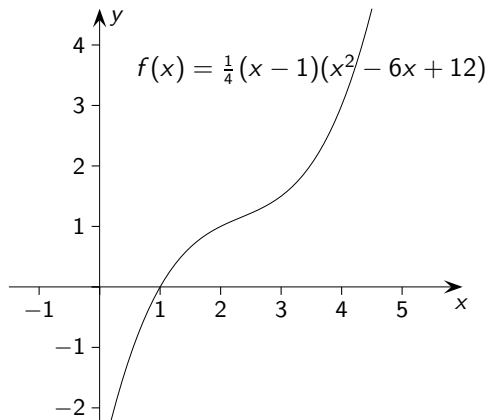
Polynom 3. Grades $ax^3 + bx^2 + cx + d$



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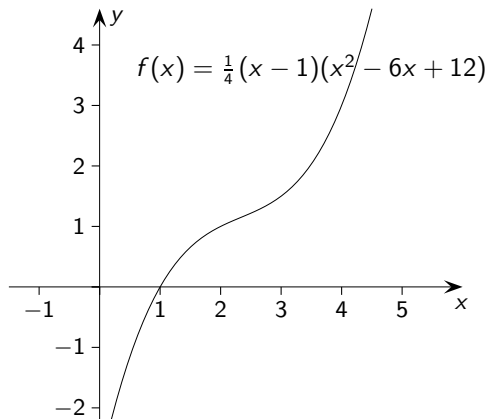


Polynom 3. Grades $ax^3 + bx^2 + cx + d$



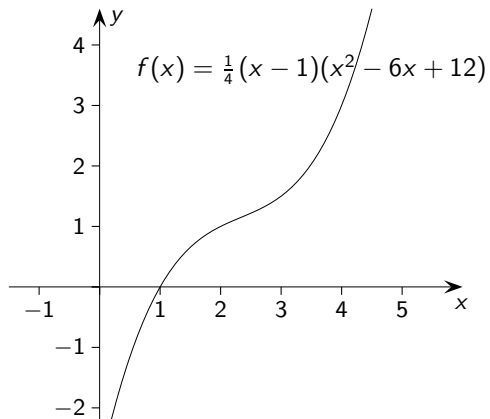
Die Zerlegung eines Polynoms 3. Grades richtet sich nach der Anzahl der Nullstellen

Polynom 3. Grades $ax^3 + bx^2 + cx + d$



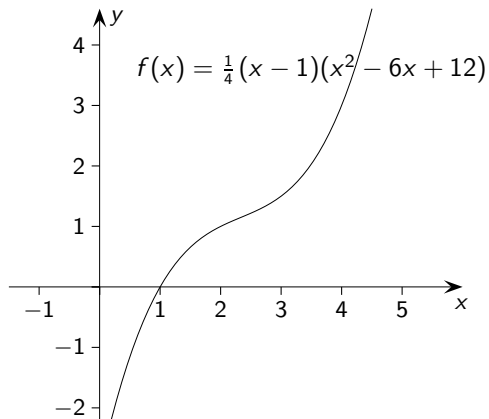
Die Zerlegung eines Polynoms 3. Grades richtet sich nach der Anzahl der Nullstellen (3, 2 oder 1) der zugehörigen Polynomfunktion. Mindestens eine Nullstelle ist vorhanden.

Polynom 3. Grades $ax^3 + bx^2 + cx + d$



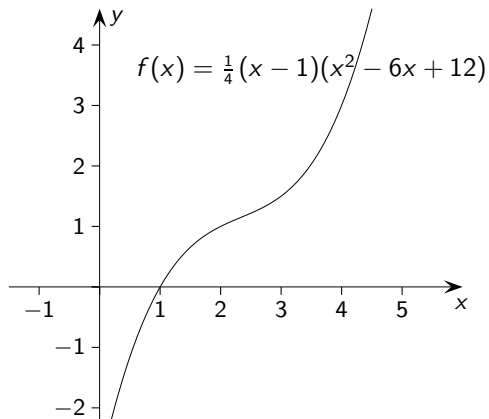
Für eine Zerlegung ist die 1. Nullstelle zu erraten. Für mögliche weitere Nullstellen ist eine

Polynom 3. Grades $ax^3 + bx^2 + cx + d$



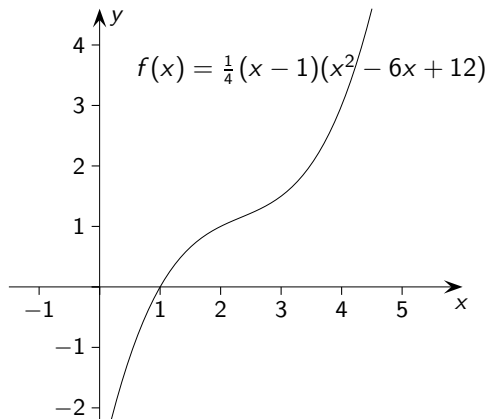
Für eine Zerlegung ist die 1. Nullstelle zu erraten. Für mögliche weitere Nullstellen ist eine Polynomdivision durchzuführen, z. B.:

Polynom 3. Grades $ax^3 + bx^2 + cx + d$



$$\frac{x^3 - 7x^2 + 8x + 16}{x + 1} = \dots = x^2 - 8x + 16 \quad \text{und} \quad x^2 - 8x + 16 = (x - 4)^2 \quad \text{mit der } pq\text{-Formel}$$

Polynom 3. Grades $ax^3 + bx^2 + cx + d$



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Insgesamt $x^3 - 7x^2 + 8x + 16 = (x + 1)(x - 4)^2$

Polynomdivision

$$(x^3 + x^2 - 10x + 8) : (x - 2) =$$

Polynomdivision

$$(x^3 + x^2 - 10x + 8) : (x - 2) = x^2$$

Polynomdivision

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$$- (\quad \quad \quad)$$

Polynomdivision

$$(x^3 + x^2 - 10x + 8) : (x - 2) = x^2$$

$$-(x^3 \quad \quad)$$

Polynomdivision

$$\begin{array}{r} (x^3 + x^2 - 10x + 8) : (x - 2) = x^2 \\ \underline{-(x^3 - 2x^2)} \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + x^2 - 10x + 8) : (x - 2) = x^2 \\ - (x^3 - 2x^2) \\ \hline 3x^2 \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + x^2 - 10x + 8) : (x - 2) = x^2 \\ - (x^3 - 2x^2) \\ \hline 3x^2 - 10x \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + x^2 - 10x + 8) : (x - 2) = x^2 + 3x \\ - (x^3 - 2x^2) \\ \hline 3x^2 - 10x \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + x^2 - 10x + 8) : (x - 2) = x^2 + 3x \\ - (x^3 - 2x^2) \\ \hline 3x^2 - 10x \\ - (\quad\quad\quad) \\ \hline \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + x^2 - 10x + 8) : (x - 2) = x^2 + 3x \\ - (x^3 - 2x^2) \\ \hline 3x^2 - 10x \\ - (3x^2 \quad \quad) \\ \hline \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + x^2 - 10x + 8) : (x - 2) = x^2 + 3x \\ - (x^3 - 2x^2) \\ \hline 3x^2 - 10x \\ - (3x^2 - 6x) \\ \hline \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + x^2 - 10x + 8) : (x - 2) = x^2 + 3x \\ \underline{-(x^3 - 2x^2)} \\ 3x^2 - 10x \\ \underline{-(3x^2 - 6x)} \\ -4x \\ \hline \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + x^2 - 10x + 8) : (x - 2) = x^2 + 3x \\ \underline{-(x^3 - 2x^2)} \\ 3x^2 - 10x \\ \underline{-(3x^2 - 6x)} \\ -4x + 8 \\ \hline \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + x^2 - 10x + 8) : (x - 2) = x^2 + 3x - 4 \\ - (x^3 - 2x^2) \\ \hline 3x^2 - 10x \\ - (3x^2 - 6x) \\ \hline -4x + 8 \\ \hline \hline \hline \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + x^2 - 10x + 8) : (x - 2) = x^2 + 3x - 4 \\ - (x^3 - 2x^2) \\ \hline 3x^2 - 10x \\ - (3x^2 - 6x) \\ \hline -4x + 8 \\ - (\quad) \\ \hline \end{array}$$

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Polynomdivision

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$$(x^3 + 6x^2 + 3x - 10) : (x + 5) =$$

Polynomdivision

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$$(x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2$$

Polynomdivision

$$\begin{array}{r} (x^3 + x^2 - 10x + 8) : (x - 2) = x^2 + 3x - 4 \\ - (x^3 - 2x^2) \\ \hline 3x^2 - 10x \\ - (3x^2 - 6x) \\ \hline -4x + 8 \\ - (-4x + 8) \\ \hline 0 \end{array}$$

$$(x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2 + x$$

Polynomdivision

$$\begin{array}{r} (x^3 + x^2 - 10x + 8) : (x - 2) = x^2 + 3x - 4 \\ - (x^3 - 2x^2) \\ \hline 3x^2 - 10x \\ - (3x^2 - 6x) \\ \hline -4x + 8 \\ - (-4x + 8) \\ \hline 0 \end{array}$$

$$(x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2 + x - 2$$

Polynomdivision

$$(x^3 + 6x^2 + 3x - 10) : (x + 5) =$$

Polynomdivision

$$(x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2$$

Polynomdivision

$$\begin{array}{r} (x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2 \\ - (\quad \quad \quad) \\ \hline \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2 \\ \underline{-(x^3 \quad \quad \quad)} \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2 \\ \underline{-(x^3 + 5x^2)} \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2 \\ - (x^3 + 5x^2) \\ \hline x^2 \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2 \\ - (x^3 + 5x^2) \\ \hline x^2 + 3x \end{array}$$

Polynomdivision

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Polynomdivision

$$\begin{array}{r} (x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2 + x \\ - (x^3 + 5x^2) \\ \hline x^2 + 3x \\ - (x^2 + 5x) \\ \hline - 2x - 10 \\ \hline - 10 \\ \hline 0 \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2 + x \\ - (x^3 + 5x^2) \\ \hline x^2 + 3x \\ - (x^2 + 5x) \\ \hline - 2x - 10 \\ \\ \hline \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2 + x - 2 \\ - (x^3 + 5x^2) \\ \hline x^2 + 3x \\ - (x^2 + 5x) \\ \hline - 2x - 10 \\ \hline \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2 + x - 2 \\ - (x^3 + 5x^2) \\ \hline x^2 + 3x \\ - (x^2 + 5x) \\ \hline - 2x - 10 \\ - () \\ \hline \end{array}$$

Polynomdivision

$$\begin{array}{r} (x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2 + x - 2 \\ - (x^3 + 5x^2) \\ \hline x^2 + 3x \\ - (x^2 + 5x) \\ \hline - 2x - 10 \\ - (-2x) \\ \hline - 10 \end{array}$$

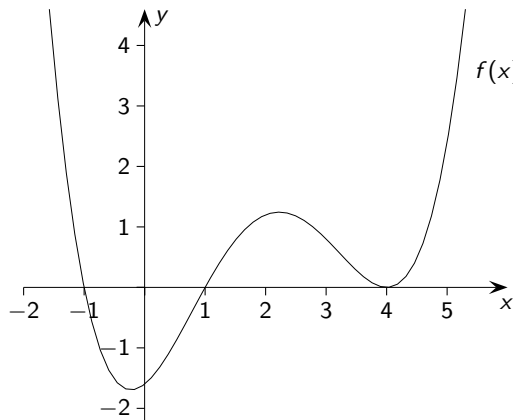
Polynomdivision

$$\begin{array}{r} (x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2 + x - 2 \\ - (x^3 + 5x^2) \\ \hline x^2 + 3x \\ - (x^2 + 5x) \\ \hline - 2x - 10 \\ - (-2x - 10) \\ \hline 0 \end{array}$$

Polynomdivision

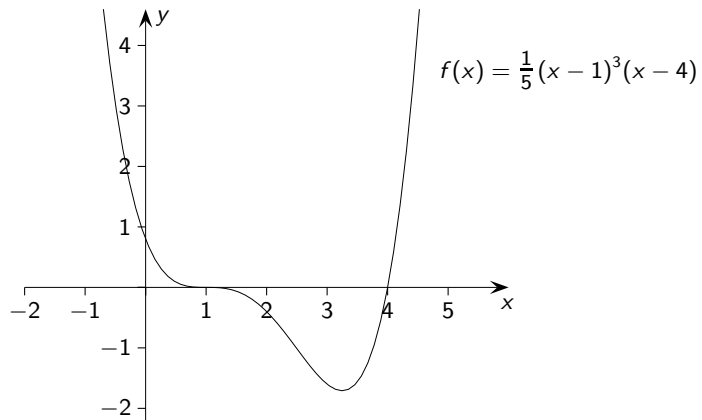
$$\begin{array}{r} (x^3 + 6x^2 + 3x - 10) : (x + 5) = x^2 + x - 2 \\ - (x^3 + 5x^2) \\ \hline x^2 + 3x \\ - (x^2 + 5x) \\ \hline - 2x - 10 \\ - (-2x - 10) \\ \hline 0 \end{array}$$

Polynom 4. Grades $ax^4 + bx^3 + cx^2 + dx + e$

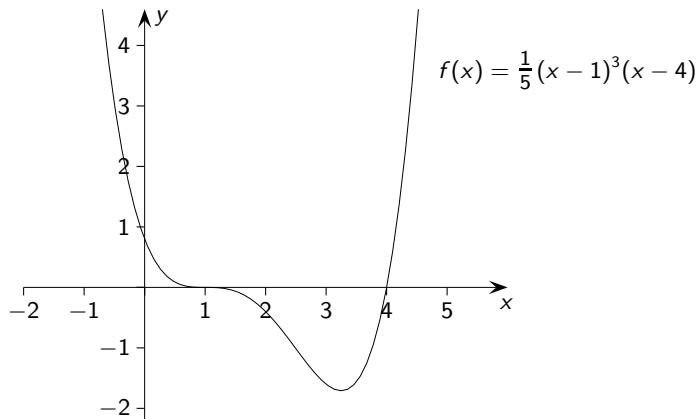


$$f(x) = \frac{1}{10}(x+1)(x-1)(x-4)^2$$

Polynom 4. Grades $ax^4 + bx^3 + cx^2 + dx + e$

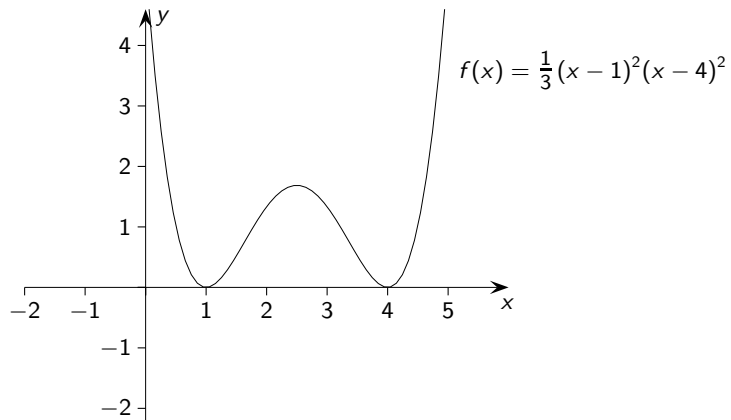


Polynom 4. Grades $ax^4 + bx^3 + cx^2 + dx + e$

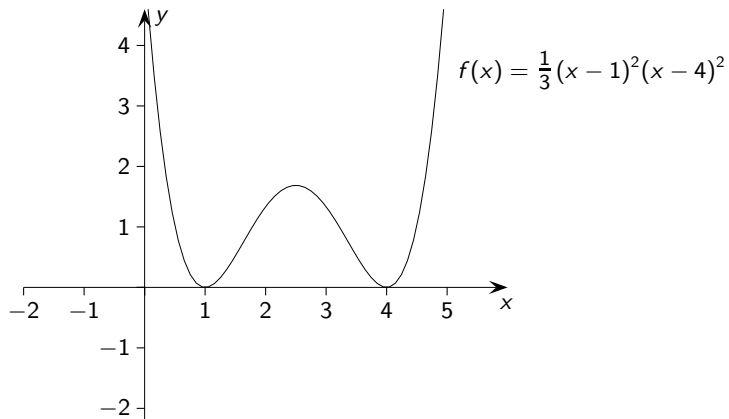


In der Umgebung von $x = 1$ ähnelt der Graph dem verschobenen Graphen von $y = -x^3$.
Beachte: In dieser Umgebung ist der Faktor $(x - 4)$ negativ.

Polynom 4. Grades $ax^4 + bx^3 + cx^2 + dx + e$



Polynom 4. Grades $ax^4 + bx^3 + cx^2 + dx + e$



In den Umgebungen von $x = 1$ und $x = 4$ ähnelt der Graph dem verschobenen Graphen von $y = x^2$. In diesen Umgebungen ist jeweils der übrige quadratische Term positiv.